

Modern Electronic Technology

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An Improved Multi-UAV Rapid Autonomous Exploration Method Based on Environmental Complexity Mode Switching

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ARTICLE INFO ARTICLE 2007 A BSTRACT

Article history Received: 25 February 2024 Revised: 1 March 2024 Accepted: 23 March 2024 Published Online: 30 March 2024

Keywords: Aerial System Perception and Autonomy Path Planning Environmental Complexity

With the continuous development of drone technology, rapid exploration strategies are of significant importance for tasks such as search and rescue and surveying. Current autonomous exploration systems often face issues of partial small-area information omission in cluttered environments, leading to repeated visits by drones. This paper proposes an improved multi-drone autonomous exploration system, which introduces a novel mode-switching mechanism based on a rapid autonomous exploration framework. This mechanism dynamically adjusts the exploration mode of the drones using the density information of surrounding obstacles. By doing so, drones can avoid missing small pieces of information that result in repeated visits in complex environments, while maintaining high exploration efficiency in simpler environments. This flexible exploration planning approach effectively addresses varying levels of environmental complexity. Evaluations conducted in three different environments of varying complexity demonstrate that the proposed method achieves higher exploration efficiency and reconstruction quality.

1. INTRODUCTION

In modern society, indoor building environments are frequently accessed by people. During disasters, minimizing secondary casualties is critical, and robots become an essential solution. Due to the lack of detailed information about the task area and the complexity of indoor environments, GPS signals often become weak or unavailable, limiting robotic search and rescue operations. In such cases, autonomous exploration and visual positioning technologies are crucial tools. Autonomous exploration enables robots to independently navigate disaster-stricken buildings, search for victims, and assess potential hazards, reducing the risk of further injuries.

Utilizing visual or radar-based positioning technologies such as VINS or SLAM, robots can accurately determine their location without GPS and build real-time maps of the environment, improving obstacle avoidance and navigation capabilities. Thus, the application of autonomous exploration technology in robots significantly enhances the efficiency and safety of rescue operations.

In recent years, Unmanned Aerial Vehicles(UAV) have demonstrated exceptional adaptability in various exploration tasks due to their small size and flexibility, particularly in complex indoor environments. These include narrow corridors and intricate stair structures filled with obstacles.

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With advanced sensing technologies, drones can autonomously plan paths, explore environments, and quickly adapt to changes, completing pre-rescue exploration tasks efficiently. This reduces the risk to rescue personnel and significantly improves the efficiency of rescue operations. As drone technology advances, the limitations of single-drone missions in largescale scenarios have led to the development of multi-drone systems. Compared to a single drone, multiple drones can cover more areas simultaneously, greatly enhancing search efficiency and reducing rescue time, making operations faster and more efficient.

This paper focuses on decentralized multidrone autonomous exploration technology, aiming to complete exploration tasks quickly in cluttered environments with unevenly distributed obstacles. The goal is to achieve comprehensive map coverage while minimizing repeated visits and task switching. We propose a mode-switching algorithm that allows drones to adaptively switch exploration modes based on their environment without changing their assigned tasks. Drones can explore quickly in simple environments and conduct detailed exploration in obstacle-dense areas to avoid missing information and repeated visits. Multi-robot coordination is achieved through direct point-to-point communication in a decentralized manner, with a task allocation module reasonably dividing the areas to be explored. We tested the proposed method in three different maze simulations, evaluating its performance. The results revealed the method's superior efficiency, achieving higher overall drone speed and shorter exploration times.

The main contributions of this paper are as follows:

- Implementing mode-switching in exploration considering the varying complexity of different areas without changing the task.
- Conducting extensive simulation evaluations demonstrating superior performance compared to existing technologies.

2. RELATED WORK

For many years, researchers have focused on mobile robot exploration in unknown environments. The current mainstream approach for autonomous exploration is frontier-based, emphasizing the planning of efficient exploration paths to create more complete maps in less time, with shorter distances, and lower energy consumption. Frontiers are defined as the boundaries between known and unknown spaces, a concept first introduced by Yamauchi et al. in 1997 $^{[1]}$. They used frontiers to identify information-rich areas and plan paths sequentially. Subsequent research introduced information gain to evaluate candidate actions and balance exploration time and information gain

based on the environment, as seen in Stachniss et al.'s work $[2-3]$.

Frontier-based methods and Next-Best-View approaches typically consider only the information gain of the next exploration viewpoint, neglecting the information gain along the path to the next viewpoint. Bircher et al. [4] proposed the Receding Horizon Next-Best-View planner (RH-NBVP), which finds the best branch in a computed random tree and repeats the process for better exploration of large environments. Some papers, like Meng et al. [5], combined frontier with sampling methods to improve computational efficiency by sampling viewpoints around the frontier. Recently, Zhou et al. [6] introduced a method using incremental frontier detection and surrounding viewpoint sampling to generate effective global paths, achieving safe and agile local exploration operations. Duberg et al. $^{[7]}$ argued that the size of the information gain is not crucial, instead selecting view-points with information gain above a threshold and then moving to the nearest one.

To further improve exploration efficiency and reduce time, early papers like [8] proposed multirobot collaboration, initially using centralized communication and task allocation via a central server. Burgard et al. $[9]$ coordinated multi-robot tasks by greedily choosing robot-target pairs based on distance and information gain. Tian et al. [10] introduced the multi-Travelling Salesman Problem (mTSP) to allocate robots to candidate frontiers. However, real-world factors like environment complexity and server reliability affect communication quality, leading to decentralized coordination methods. The first decentralized multi-robot exploration, developed by Palazzolo et al. [11], had robots share map information and move to the nearest frontier. Despite its simplicity, coordination was ineffective without central control. Kabir et al. [12] and Yu et al. [13] proposed methods to mitigate these issues, but required stable communication. Klodt et al. [14] reduced communication dependency through pairwise interactions, and Zhou et al. $[15]$ introduced a method to divide navigation areas and ensure different exploration regions, enhancing robustness for limited communication.

However, Bartolomei et al. [16] highlighted that Zhou's method assumes uniform obstacle distribution, leading to decreased coordination in cluttered environments and leaving unexplored islands. They proposed a flexible task-switching navigator to address this, changing some UAVs' tasks to clear unknown spaces. This improved efficiency but altered local tasks. To avoid this, we developed a new mode-switching method that adjusts path planning costs based on environmental complexity, ensuring slow and cautious exploration in complex environments to

avoid missing small areas and reducing repeated visits. This approach enhances task efficiency without changing UAV tasks.

3. METHODOLOGY

3.1 System Overview

The overall system design is depicted in Figure 1. This study focuses on exploring unknown environments with communication constraints using UAVs equipped with front-facing depth cameras. We employ the Visual-Inertial Navigation System (VINS) method as outlined in $[17]$ for distributed state estimation, ensuring accurate localization of both self and other quadcopters.

Our approach utilizes a decentralized coordination strategy where agents exchange map information, viewpoints, execution modes, and planned trajectories to allocate exploration areas and collaborate on map construction. Each UAV operates through a pipeline consisting of three main components: mapping system, collaborative task allocator, mode selector, and path planner.

Inspired by reference $\begin{bmatrix} 16 \end{bmatrix}$, we have also developed a mode-switching algorithm. The mapping system generates a voxel grid map of the environment using odometry and depth information $[30]$. With each update, newly observed we design the CVRP formula. Suppose voxels are stored in blocks and communicated to nearby grid cells and N_x UAV nodes. The relevant UAVs. Next, Frontiers are extracted and clustered. Sub-
 $C_{\alpha v r p} \in \mathbb{R}^{(N_g + N_x + 1) \times (N_g + N_x + 1)}$ is as follows: sequently, using paired interactions and the Capacitated Vehicle Routing Problem (CVRP) formula^[15], UAV tasks are coordinated. Upon receiving their respective tasks, nteractions and the C
(CVRP) formula ^[15],
eceiving their respec \mathbf{C} **VRP**) formula^[15], **UAV** task

UAVs plan exploration routes, extracting frontier information to identify viewpoints at boundaries between known and unknown maps.

Time lower bounds related to path time cost and angular velocity cost are obtained using ATSP to stratify UAVs for global and local path planning. The mode switcher determines mode switching based on the density of surrounding obstacles. Specifically, point cloud information from the mapping system is used to extract obstacle information. Gaussian distribution sampling is performed on this information to determine obstacle density, dynamically triggering mode switches. Different modes assign varying speeds, task boundaries, and proportions of path time cost and angular velocity cost to UAVs.

3.2 Multi-Task Allocation

In this study, we adopt the Hgrid map division method mentioned in $[2]$. For multi-task allocation, we employ the vehicle routing problem (VRP). In a standard VRP, routes form closed loops from a central depot. However, since exploration tasks lack a central depot, ^[2] introduces a virtual depot and designs connection costs to reduce this $\frac{1}{2}$ men of the environment varies edemotry and variant to an asymmetric VRP. Following this approach, I map of the environment using odometry and
mation $\frac{1}{2}$ ^[30]. With each undate, newly observed we design the CVRP formula. Suppose there are N_g grid cells and N_r UAV nodes. The relevant cost matrix $C_{avrn} \in \mathbb{R}^{(N_g + N_x + 1) \times (N_g + N_x + 1)}$ is as follows:

$$
C_{\text{avpp}} = \begin{bmatrix} 0 & -\mathbf{Inf}_{d,x} & \mathbf{Inf}_{d,g} \\ \mathbf{Inf}_{d,x} & \mathbf{Inf}_{x} & \mathbf{C}_{x,g} \\ 0 & 0 & \mathbf{C}_{g} \end{bmatrix}
$$
 (1)

Figure 1. Overview of the Multi-UAV Autonomous Exploration System.

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Modern Electronic Technology | Volume 08 | Issue 01 | March 2024
Formula 1 represents a basic CVRP cost matrix. Since cluster. The cost from the current position Formula 1 represents a basic CVRP cost matrix. Since drones do not need to return to the same point, all diagonal elements of the cost matrix are set to 0. In this ma-
formula $k \in [1, N_{cls}]$ trix, $-\text{Inf}_{d,x}$ denotes the connection cost from the virtual $M_{t=0}(0,k) = t_n(\mathbf{x}_0, \mathbf{x}_1) + w_{t=0} \cdot t_{t=0}(\mathbf{x}_1)$ (5) depot to all drones, set to a large negative value to allow $\frac{1}{\sqrt{2}}$ direct connections between the virtual depot node and the drones. **Inf**_{*d_s*} and **Inf**_{*dx*} represent the connection costs from the virtual depot to grid cells and from drones to the virtual depot, respectively, both set to a large positive
target direction where v_0 is the current ve value to prohibit infeasible paths. Inf_x represents the connection costs between different drones, with all elements $t(x) = cos^{-1} \frac{(p_{k,j} - p_0) \cdot v_0}{r}$ (6) except the diagonal set to a large positive value to indicate except the diagonal set to a large positive value to indicate
infeasible paths. $C_{x,g}$ denotes the connection costs between drones and grid cells, while C_g represents the connection costs between grid cells, typically calculated using the speed of the drone. path length $Len(\cdot)$. drones do not need to return to the same point, all diag-
the N_{fir} clusters is calculated as shown in Formula 5(In the dictions. \mathbf{m}_{dg} and \mathbf{m}_{g} C݃ represents the connection costs between grid cells, typically calculated using the path length *Len*(·). $\frac{1}{2}$ and $\frac{1}{2}$ routes for a standard vehicle loops for $\frac{1}{2}$ routes for a central depot. However, $\frac{1}{2}$ and the depotes. $\mathbf{m}_{d,g}$ and v_{ref} and the large negative value to allow direct connections between the virtual depoted value to allow direct connections between the virtual depoted value of v_{ref} pain iongul $Len()$. Formula 1 represents a basic CVRP cost matrix. Since cluster. The cost from the current position

3.3 Exploration Planning \mathcal{C} . Exploration 1

since exploration tasks lack a central depot, [2] introduces a virtual depot and designs connection costs to reduce

In this paper, the boundary is obtained using the meth-
into a od in $^{[6]}$. Then, sampling is performed uniformly in a cy-necting the closed loop path does not affection. lindrical coordinate system centered at the cluster center to obtain viewpoints with coverage angles greater than the threshold. The angle with the largest coverage is selected as the angle bound to the viewpoint. Each viewpoint $q_{i,j}$ is represent bother clusters: represented by its position and yaw angle $\{x_{i,f}, \varphi_{ij}\}$. $rac{6}{100}$ epresented by its position and yaw angle $\{x_{i,f}, \varphi_{ij}\}\$.
 $C_f(k_1, k_2) = t_{lb}(\mathbf{q}_{k_1,1}, \mathbf{q}_{k_2,1}), k_1, k_2 \in [1, N_{\hat{j}_{tr}}]$ connection costs between grid cells, typically connected using the path *Length* **The path of the path of the path in** ω obtain viewpoints w external coordinate syst

need to be taken into account for path planning in vari-
the need to revisit less explored areas 1) Fast Exploration Mode: Driven by frontiers, the goal of the fast exploration mode is to cover large previously $\frac{1}{\pi}$ ration mode aims to avoid small une unknown areas quickly. Considering that different factors complex environments as much as nos $\frac{1}{2}$ ous environments, we processed the most important time cost t_{lb} from ^[6], changing the original method of directly selecting the maximum of the path time cost $T_{L, cost}$ and the turning time cost $T_{\varphi, cost}$ to a weighted sum method: cost t_{lb} from $\ddot{\ }$, changing to 1) Fast Exploration Mode: Driven by frontiers, the goal 2) Cautious Exploration Mode: The $\sum_{t\in I}$ \cdots \cdots \cdots costs more significant. In cautious explored areas the need to revisit less explored areas and anti-

$$
t_{lb}(\mathbf{x}_{k_1,j_1}, \mathbf{x}_{k_2,j_2}) = w_L T_{L, cost} + w_T T_{\varphi, cost}
$$
 (2)

$$
T_{L, \text{cost}} = \frac{Len[P(\mathbf{x}_{k_1, j_1}, \mathbf{x}_{k_2, j_2})]}{v_{max}}
$$
(3)

$$
T_{\varphi, \text{cost}} = \frac{\min(|\varphi_{k_1,j_1} - \varphi_{k_2,j_2}|, 2\pi - |\varphi_{k_1,j_1} - \varphi_{k_2,j_2}|)}{\mathbf{\mathcal{B}}_{\text{max}}}
$$
(4)

 $T_{L, cost}$ and $T_{\varphi, cost}$ represent the path time cost and turning time cost respectively. w_L and w_T are their respective weights. In fast exploration mode, we set a higher weight for the path time cost w_L and a smaller weight for the turning time cost w_T . This encourages the drones to explore unknown areas more greedily, similar to the approach described in the paper [7], thereby improving exploration efficiency.

> Subsequently, following the method outlined in $[6]$, we constructed an Asymmetric Traveling Salesperson Problem (ASTP) to find a complete path passing through each

cluster. The cost from the current position $x_0 = (p_0, \varphi_0)$ to diagonal elements of the cost matrix $\alpha \in [1, N_{cls}]$, α (p_0, φ_0) to formula $k \in [1, N_{cls}]$

$$
M_{\text{top}}(0,k) = t_{lb}(\mathbf{x}_0, \mathbf{x}_{k,1}) + w_{\text{con}} \cdot t_{\text{con}}(\mathbf{x}_{k,1})
$$
\n(5)

I depot node and To achieve more consistent movement and limit exrepresent connection costs between different drones, avoiding UAVs from frequently switching between different target points with similar t_b values, we denote the connection costs between different target points with similar t_b values, we om the virtual depot to grid cents and from drones to
he virtual depot, respectively, both set to a large positive α consistent movement and limit excessive turns, avoid α values, we calculate the angle between the angle between the angle between the angle between the current direction and the current direction and the current direction and the angle between \mathcal{L} target direction, where v_0 is the current velocity:

$$
t_{con}(\mathbf{x}_{k,j}) = cos^{-1}\frac{(p_{k,j} - p_0) \cdot v_0}{\|p_{k,j} - p_0\| \|v_0\|}
$$
 (6)

 v_0 is the Here, p_{kj} represents the current position of the drone, p_0 is the position of the drone before it moved, and v_0 is the speed of the drone.

The cost between each cluster and the current position The cost between each cluster and the current position is the current position is the exploration of the exploration α $\frac{1}{\sqrt{2}}$ α Discon timality **3** Exploration Planning x_0 is then uniformly set to 0. This avoids the exploration task forming task forming a closed loop, allowing it to be converted to be converted into a traditional ATSP problem for processing. Disconnecting the closedloop path does not affect the optimality of the result.

e is selected tion costs between clusters, primarily the time cost from. $\frac{1}{2}$ and $\frac{1}{2}$ for $\frac{1}{2}$ for $\frac{1}{2}$ for $\frac{1}{2}$ and $\frac{1}{2}$ for $\frac{1}{2}$ f C_f is the main symmetric block recording the conneceach cluster to other clusters:

$$
\mathbf{C}_{f}(k_{1},k_{2}) = t_{lb}(\mathbf{q}_{k_{1},1},\mathbf{q}_{k_{2},1}), k_{1},k_{2} \in [1,N_{\text{fir}}]
$$
(7)

of the turning time cost w_T and decreasing the weight of tiers, the goal α of the fast exploration mode is to cover large in the fast exploration mod bifus, the goal and α cautious Exploration Mode: The cautious exploration mode aims to avoid small unexplored areas in different factors μ and time complex environments as much as possible, preventing μ ous exploed areas in simple or open environments, drones can fly and explore in straight paths, with α preventing path costs generally more in contract than that the set of the costs. However, in contract than the set of the contract than that the contract than the contract than the costs. However, in contract than the cont s map after ents, drones reduce their modes, $r = r$ the need to revisit less explored areas on the map after the mission ends. In simple or open environments, drones can fly and explore in straight or near-straight paths, with small turns, making path costs generally more important than turning costs. However, in complex environments, such as narrow urban streets, forests, or building interiors, frequent turns and obstacle avoidance make turning costs more significant. In cautious exploration mode, drones reduce their maximum speed v_{max} and adjust the weights in the time lower bound function, increasing the weight the path time cost w_L . This gives a new time lower bound t_{lb} , which is then used in the ATSP formula, making the drones explore more cautiously, reducing missed information. This also avoids large turns, maintaining safety while exploring unknown areas as thoroughly as possible.

3.4 Environmental Complexity Mode Switching

In both exploration and planning tasks, assessing environmental complexity is crucial as it directly impacts robot performance, task success rates, and resource consumption. For instance, as discussed in $[18]$, environmental complexity is determined by the number of obstacles surrounding the drone. In this study, we simplify obstacle detection using point cloud data segmentation, where obstacles are reduced to points to determine levels of environmental complexity. We employ a region growing algorithm for cluster segmentation,

(b) Sampling Points tion Extraction. Visualization ity levels between H_{min} and H_{max} mode **Figure 2.** Extraction and Augmentation of Environmental directly triggered. Information: In figure (a), the green points represent the clustering results, while in figure (b), the small points of various colors represent the Gaussian distribution samresults, while in figure (b), the small points of various results. **(a)** Obstacle Informa- **(b)** Sampling Points tion Extraction. Visualization.

performance, task success rates, and resource consumption. For instance, as discussed in [18], environmental

dividing the point cloud data *P* into *n* subregions $P_1, P_2, ..., P_n$, each representing a distinct obstacle. **(a)** Obstacle Informa- **(b)** Sampling Points tion Extraction. Visualization.

ing significantly reduces the data to be processed. To points to obtain *N* three masses in the set processes in the obtain more usable information for subsequent analysis, we randomly sample around these simplified obstacle mean of the sampling po points to obtain N threedimensional sampling points $X = \{(x_i, y_i, z_i)\}_{i=1}^N$, which follow a multivariate normal dis $triv \overrightarrow{u} \overrightarrow{u}$, \overrightarrow{v} , $\$ points to obtain *N* infectimentional samplif reducing obstacts information to points via cruster $\sum_{i=0}^{n} (l-i)$ R_{data} is the obstacle in N_{data} compling noints the data to be property reduces the data to be processed. To be provided the data to be provided to be pro points to both it incommension sampling points n_{min} and n_{max} . $X = \{(x_i, y_i, z_i)\}_{i=1}^{\infty}$, which follow a multivariate normal dis-
tribution $N(u, \Sigma)$

 T_{rel} instituted by (μ, Δ) . a square sharing while we centered at the current arole and the two tion mode, it should switch to c
position x_{new} to delineate local environmental regions for $\qquad \qquad \text{mode}$. plexity using information entropy. Specifically, we assume each dimension is divided into $n_x n_y n_z$ grids. We initialize probability distribution of the sampling points in each grid: $\frac{1}{2}$ erse all sampling points. Based on their grid indices, we mode. Taking inspiration from $^{[19]}$, in this study, we construct cluttered environment. If the UA a square sliding window centered at the current drone tion mode it should switch to c position x_{new} we define the corresponding the matrix in the matrix $\text{mod}e$. a three-dimensional matrix **G** of size $n_x \times n_y \times n_z$ and travincrement corresponding counts in the matrix. probability distribution of the sampling points in each grid: computation purposes. We measure environmental com-

• I

$$
index_{x} = \left[\frac{\mathbf{x}_{i} - \mathbf{x}_{min}}{\Delta \mathbf{x}} \right]
$$
 (8)

Based on their grid indices, we increment corresponding counts in the matrix.

Based on their grid indices, we increment corresponding counts in the matrix.

where ϵ Here, x represents the coordinates of the sampling points. Afon growing containing the number of sampling points in each grid. We calculate the number of sampling points in each grid. We p_1 become sampling points in each grid: p_1 and p_2 grid: p_3 grid: p_4 grid: p_5 grid: p_6 grid: p_7 grid: p_8 grid: p_7 grid: p_8 grid: p_9 grid: p_9 grid: p_9 grid: p_9 grid: p_9 grid: ts in each g μ points in each grid. points in each p θ *i* θ *i* **G** points in each grid: ter traversal, we obtain the matrix G (index_{xx}, index_{xy}, index_{yy}) then calculate the probability distribution of the sampling
 D

$$
P_{ijk} = \frac{\mathbf{G}(i, j, k)}{\sum_{i=0}^{n_x - 1} \sum_{j=0}^{n_y - 1} \sum_{k=0}^{n_z - 1} \mathbf{G}(i, j, k)}
$$
(9)

with the sliding window: where *Pijk* is the probability of sampling points in the (i,j,k) grid. Next, we calculate the information entropy within the sliding window:

$$
H = -\sum_{i=0}^{n_x - 1} \sum_{j=0}^{n_y - 1} \sum_{k=0}^{n_z - 1} P_{ijk} \log (P_{ijk} + \phi)
$$
(10)

To avoid $log(0)$, a small value ϵ is added. The resulting information entropy represents the environmental complexity

In specific exploration tasks, When the environmental in specific exploration tasks, When the environmental in specific exploration dasks, when the chylominental complexity within the UAV's sliding window exceeds a $\sum_{m,n=1}^{\infty}$ is less than H_{min} indicating a low-complexity environment, the UAV switches to fast exploration mode. For complexcomplexity is determined by the number of obstacles surrounding the drone. In this study, we simplify observation $\frac{1}{2}$ Complexity within the UAV is shung whithew exceeds a
throubold II indicating a high complexity environment threshold H_{max} , indicating a high-complexity environment, the UAV switches to cautious exploration mode. Conversely, if the number of sampling points around the UAV d. Instead, we si e based on the rate sampling points within the UAV's sliding window. The directly triggered. Instead, we simulate the complexity change rate based on the rate of change in the number of complexity change rate based on the rate of change in the number of In specific exploration the exploration tasks, The employees the environmental complexity levels between H_{min} and H_{max} mode switching is not where where the mean of the mean of the time series, and $\frac{1}{n}$ in $\frac{1}{n}$ pling point changes determine whether to switch modes. UAV's previous exploration mode and the trend in sam-The rate of change *a* is calculated as follows: a threshold we can H_{min} and H_{max} , mode switching is not $\frac{1}{2}$ follows:

$$
P_1, P_2, ..., P_n, \text{ each representing a distinct obstacle.}
$$

Reducing obstacle information to points via cluster-
ing significantly reduces the data to be processed. To

$$
a = \frac{\sum_{i=0}^{k-1} (i - \overline{t})(n_{i-i} - \overline{n})}{\sum_{i=0}^{k-1} (i - \overline{t})^2}
$$
(11)

where \bar{t} is the mean of the time series, and \bar{n} is the mean of the sampling points. The slope a indicates the trend. When the number of sampling points is between
 \mathbf{r} , and \mathbf{r} , it n_{min} and n_{max} . n_{max} is in fact the UAV is in fact to causal switch to causal swit n_{min} and n_{max} .

- and exceeds h_{thr} it suggests the UAV has entered a tion mode, it should switch to cautious exploration
mode cluttered environment. If the UAV is in fast explora- \Box mode. mode.
- If $a < 0$, indicating a decrease in sampling points, $\frac{1}{2}$ e an open environment. If the UAV is in cautious exploration mode, it should switch to fast exploration of 5m. The maximum linear andangular velocities of the drones are set to 1*.*5*m/s* and 0*.*9*rad/s*, respectively. We and is below l_{thr} , it suggests the UAV has entered mode.
- increment corresponding counts in the matrix.
 \bullet If a is between n_{thr} , and l_{thr} , the environmental change • If *a* is between h_{thr} , and l_{thr} , the environmental change

is not significant, and the UAV continues in its current mode without switching.

The thresholds h_{thr} , and l_{thr} are small positive and negative values of equal magnitude, respectively. This method ensures efficient mode switching based on real-time environmental complexity, optimizing the UAV's exploration efficiency.

4. EXPERIMENTS

4.1 Results of Different Multi-UAV Exploration Methods in Various Environments

To evaluate the performance and feasibility of the proposed method, we used the dynamics simulator from [15] for simulation. Each agent is equipped with a forward-facing depth camera with a resolution of 640×480 pixels and a field of view of $80° \times 60°$. Depth images are processed using the method in $[17]$, with a maximum perception range of 5m. The maximum linear and angular velocities of the drones are set to 1*.*5*m/s* and 0*.*9*rad/s*, respectively. We

compared the exploration process with RACER^[15] and a Ufoexplorer-like algorithm $[7]$ to verify the time required to complete scene exploration and the completeness of the established map. The core of the Ufoexplorer algorithm is selecting the nearest viewpoints; in our experiments, we implemented this by setting the path cost weight to 1 and the corner cost weight to 0.

We tested three scene sizes: a simple maze with dead ends 20*m*×20*m*×2*m*, a more complex maze with dead ends and loops $30m \times 16m \times 2m$, and a highly cluttered maze with unevenly distributed obstacles $20m \times 14m \times 2m$.

 (a) Simple **(b)** Complex **(c)** Highly **Figure 3.** Three schematic diagrams depicting mazes of varying complexity.

Through testing each algorithm in different environments, we obtained the results shown in the Table 1.

Table 1. Map coverage and exploration efficiency data achieved by different numbers of drones using different methods in different environments.

num		Simple		Complex		Highly Complex	
1	RACER	$96.16\% \pm 1.52\%$	$111.16s \pm 10.15$	$96.61\% \pm 1.61\%$	$114.15s \pm 10.21$	$96.34\% \pm 1.76\%$	$116.23s \pm 10.12$
	Ufoexplorer	$96.14\% \pm 1.24\%$	$110.31s \pm 9.75$	$96.10\% \pm 1.65\%$	$117.36s \pm 11.02$	$96.01\% \pm 1.81\%$	$121.80s \pm 11.41$
	Ours	$97.33\% \pm 0.51\%$	$95.24s \pm 5.17$	$97.42\% \pm 0.53\%$	$103.98s \pm 5.23$	$97.46\% \pm 0.63\%$	$91.31s \pm 5.14$
2	RACER	$96.19\% \pm 1.31\%$	$97.69s \pm 10.05$	$96.69\% \pm 1.60\%$	$99.19s \pm 10.07$	$96.40\% \pm 1.71\%$	$101.33s \pm 10.13$
	Ufoexplorer	$96.21\% \pm 1.21\%$	$95.50s \pm 9.51$	$96.17\% \pm 1.62\%$	$102.21s \pm 10.53$	$96.21\% \pm 1.79\%$	$107.65s \pm 10.21$
	Ours	$98.04\% \pm 0.45\%$	$76.82s \pm 5.04$	$98.03\% \pm 0.43\%$	$79.68s \pm 4.91$	$97.46\% \pm 0.57\%$	$74.62s \pm 4.87$
4	RACER	$96.46\% \pm 1.28\%$	$76.15s \pm 9.34$	$96.72\% \pm 1.31\%$	$79.21s \pm 9.65$	$96.79\% \pm 1.48\%$	$78.70s \pm 9.62$
	Ufoexplorer	$96.63\% \pm 1.17\%$	$73.13s \pm 9.12$	$96.52\% \pm 1.38\%$	$83.12s \pm 9.78$	$96.49\% \pm 1.63\%$	$84.75s \pm 9.77$
	Ours	$98.24\% \pm 0.43\%$	$65.42s \pm 4.56$	$98.31\% \pm 0.42\%$	$68.42s \pm 4.71$	$98.23\% \pm 0.51\%$	$62.37s \pm 4.09$
6	RACER	$96.82\% \pm 1.19\%$	$67.31s \pm 9.12$	$96.94\% \pm 1.28\%$	$69.74s \pm 9.15$	$96.61\% \pm 1.49\%$	$68.72s \pm 9.08$
	Ufoexplorer	$96.99\% \pm 1.16\%$	$64.14 \pm 8.98s$	$96.56\% \pm 1.31\%$	$73.14s \pm 9.41$	$96.64\% \pm 1.52\%$	$75.71s \pm 9.16$
	Ours	$98.23\% \pm 0.47\%$	$61.48s \pm 4.12$	$98.21\% \pm 0.43\%$	$63.07s \pm 4.67$	$98.12\% \pm 0.52\%$	$56.83s \pm 4.11$
8	RACER	$96.36\% \pm 1.49\%$	$65.11s \pm 9.21$	$96.72\% \pm 1.42\%$	$69.12s \pm 9.72$	$96.52\% \pm 1.53\%$	$67.79s \pm 9.12$
	Ufoexplorer	$96.32\% \pm 1.38\%$	$62.68s \pm 8.03$	$96.64\% \pm 1.45\%$	$72.71s \pm 10.13$	$96.43\% \pm 1.57\%$	$74.12s \pm 9.29$
	Ours	$98.13\% \pm 0.49\%$	$58.28s \pm 3.98$	$98.19\% \pm 0.47\%$	$62.15s \pm 4.93$	$98.21\% \pm 0.61\%$	$56.75s \pm 4.41$

Figure 4: Illustration of exploration efficiency achieved by different numbers of drones using different methods in different environments.

From Figure 3, it is evident that in relatively simple environments, the efficiency of Ufoexplorer, which considers only path costs, is superior to RACER. This is because in simple environments, which are mostly open spaces, Ufoexplorer greedily explores based on path costs. However, during experiments, it was found that Ufoexplorer struggles more than RACER when encountering dead ends, resulting in similar performance between the two algorithms overall. RACER considers both path costs and the maximum angle cost, prioritizing lowering the path cost when facing dead ends to swiftly find an escape route. Continuously prioritizing low path costs might lead the drone to repeatedly attempt to navigate out of dead ends without making necessary turns.

Therefore, compared to Ufoexplorer, our mode-switching approach takes such situations into account. It not only enables fast exploration in open spaces similar to Ufoexplorer but also efficiently navigates out of dead ends akin to RACER, achieving higher exploration efficiency. In more complex mazes with numerous obstacles, the importance of angle costs becomes more apparent to enhance exploration efficiency and flight stability. Hence, in such scenarios, RACER generally outperforms Ufoexplorer. However, our mode-switching improvement method also performs reliably in complex environments with multiple obstacles, maintaining stable completion of exploration tasks.

In the last type of maze, characterized by numerous unevenly distributed obstacles, we designed the environment with partial open spaces and partially complex and uneven areas. Despite this map being the smallest, exploration time is longer compared to the previous two maps for both RACER and Ufoexplorer. Our modeswitching improvement method balances path costs and angle costs during operation, thereby achieving better operational efficiency. Additionally, by observing the error values of different algorithms, it is clear that our designed algorithm not only outperforms others in terms of performance but also exhibits superior stability during operation. Lower and less fluctuating error values indicate consistent efficiency and reliability over prolonged operation.

Overall, these analytical results thoroughly demonstrate the superiority and practicality of our algorithm. By offering higher exploration efficiency and more stable operational performance, our algorithm provides a more efficient and reliable solution for multi-UAV cooperative exploration tasks.

4.2 The impact of environmental complexity measurement methods

To demonstrate the effectiveness of the entropybased environmental complexity measurement method used in this experiment, we conducted tests using four UAVs in the three environments from the previous experiments. We

compared the efficiency of the Hamming distance method, the obstacle density method, and the entropy method as outlined in [18]. The results are presented in Table 2.

Table 2. Exploration efficiency data of four drones under different environmental measurement methods.

method	Simple	Complex	Highly Complex
Hamming distance		$70.75s \pm 6.86$ $74.42s \pm 5.51$	$72.71s \pm 6.61$
Obstacle density		$70.36s \pm 7.56$ $75.42s \pm 7.98$	$74.93s \pm 8.39$
Information Entropy	$65.42s \pm 4.56$ $68.42s \pm 4.71$		$62.37s \pm 4.09$

As shown in Figure 5, We used information entropy as a measure of environmental complexity, which outperformed Hamming distance and obstacle density methods in all three types of environments. The error bars in the figures also indicate better stability. Unlike the Hamming distance, which only compares differences between rows and columns within a sliding window, we represent obstacles as ones and free spaces as zeros in a binary pixel matrix, treating uncertain areas in unknown environments as zeros like free spaces. While the Hamming distance method performs better than simple obstacle density in complex and moderately complex environments, it doesn't consider the probability distribution and uncertainty of the data, making it less comprehensive in reflecting environmental complexity. Thus, the information entropy method is more effective in measuring environmental complexity.

5. CONCLUSIONS

The primary objective of our work is to develop a multi-UAV autonomous exploration system capable of completing environment exploration in complex settings with numerous and unevenly distributed obstacles while ensuring map integrity. To achieve this, we have incorporated a modeswitching feature into the rapid autonomous exploration framework. This feature leverages the reconstructed spatial information from the mission, analyzes surrounding obstacle information to determine environmental complexity, and adaptively switches modes based on the complexity and previous mode.

Through this mode-switching system, UAVs can autonomously balance cautious exploration of unknown spaces with more aggressive exploration. This approach enhances the efficiency and reliability of multi-UAV cooperative exploration in complex environments while maintaining rapid exploration in simpler environments. In the future, we plan to apply more advanced reinforcement learning methods to improve the accuracy of UAV environmental assessments. Additionally, we intend to implement our current method in search and rescue systems to validate the feasibility and superiority of the rapid autonomous exploration approach in real-world applications.

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